

Two warm up exercises
done before we went
through 6.2 exercises
from the text.

NOTES 12/6/11 CALCULUS

A Differential Equation is:
an equation that has a derivative in it.

A Second Order Differential Equation is:
an equation with a second derivative in it.

$$f''(x) \quad D_x^2 y$$

$$d^2y/dx^2$$

Solve $\frac{dy}{dx} = 2^x + x^2$

$$y = \frac{2^x}{\ln 2} + \frac{1}{3}x^3 + C$$

What does it mean to solve a D.E.?

Find the function which satisfies the D.E. + any other conditions given.

Now solve it with an initial condition (or boundary condition) of (1,3). ~ helps solve for C.

$$3 = \frac{2^1}{\ln 2} + \frac{1}{3} \cdot 1^3 + C$$

$$C = \frac{8}{3} - \frac{2}{\ln 2}$$

$$y(x) = \frac{2^x}{\ln 2} + \frac{x^3}{3} + \frac{8}{3} - \frac{2}{\ln 2}$$

Solve $\frac{dy}{dx} = 3x$

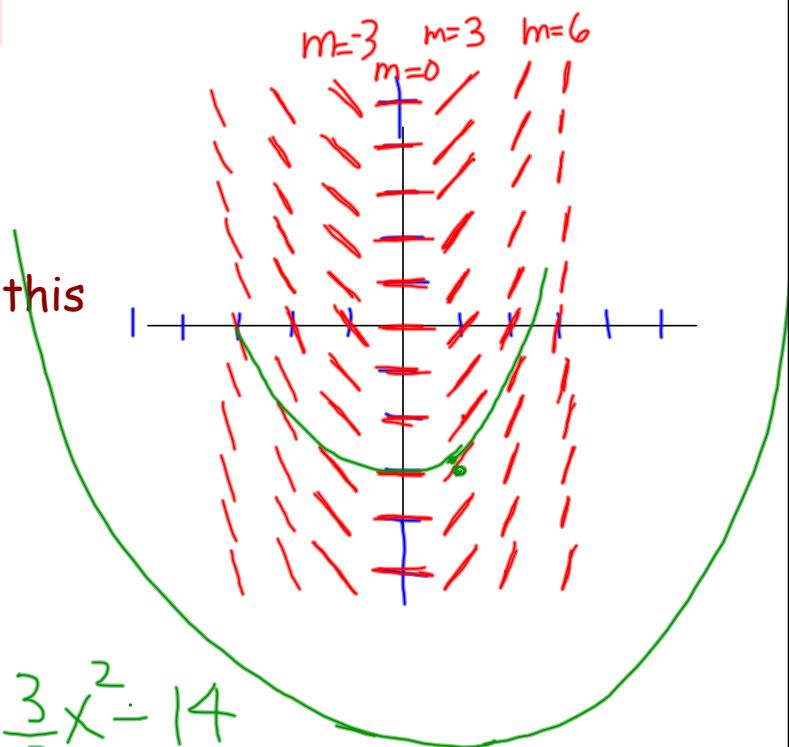
$$y = \frac{3}{2}x^2 + C$$

Create a slope field for this differential equation.

generated by a diff. eq
& it gives us a
peek at the solution's graph

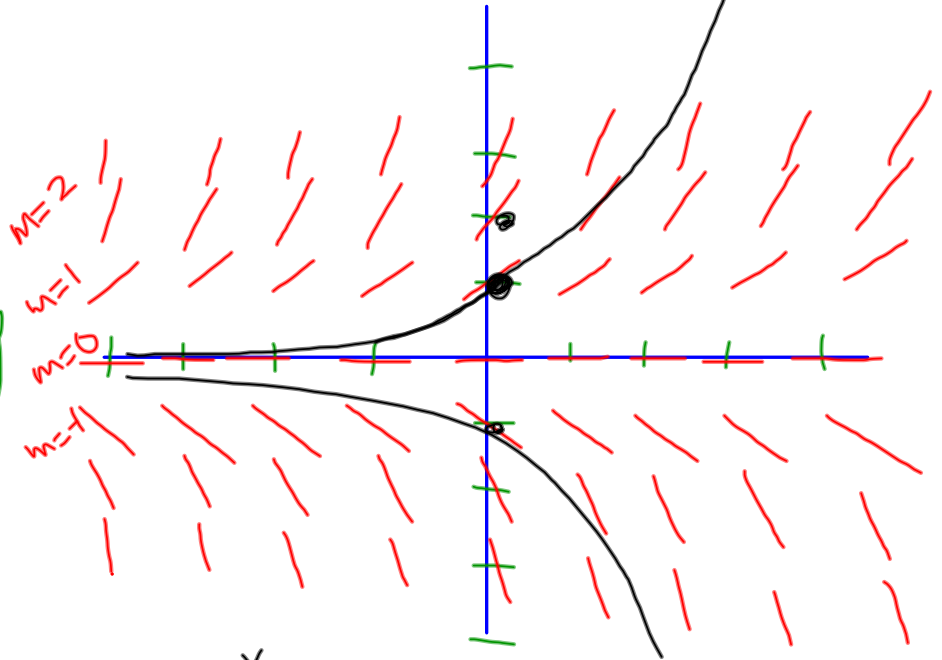
Solve $\frac{dy}{dx} = 3x$ if $y(4) = 10$

$$10 = \frac{3}{2}(4^2) + C \quad y = \frac{3}{2}x^2 - 14$$
$$-14 = C$$



Draw
a slope
field for

$$\frac{dy}{dx} = y$$



exponential
function.

$$e^x$$
$$-e^x$$
$$2e^x$$

$$y = Ke^x$$

$$\frac{dy}{dx} = Ke^x$$