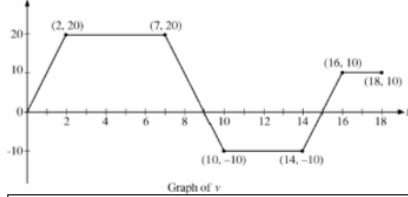


Work on these problems in your group, but show all your groups' thoughts and conclusions on your own paper. The first two problems are to be done without a calculator.

Let f and g be the functions defined by $f(x) = \frac{1}{x}$ and $g(x) = \frac{4x}{1+4x^2}$, for all $x > 0$.

- 1) Find the absolute maximum value of g on the open interval $(0, \infty)$ if the maximum exists. Find the absolute minimum value of g on the open interval $(0, \infty)$ if the minimum exists. Justify your answers.

2)



A squirrel starts at building A at time $t = 0$ and travels along a straight, horizontal wire connected to building B . For $0 \leq t \leq 18$, the squirrel's velocity is modeled by the piecewise-linear function defined by the graph above.

- At what times in the interval $0 < t < 18$, if any, does the squirrel change direction? Give a reason for your answer.
- At what time in the interval $0 \leq t \leq 18$ is the squirrel farthest from building A ? How far from building A is the squirrel at that time?
- Find the total distance the squirrel travels during the time interval $0 \leq t \leq 18$.
- Write expressions for the squirrel's acceleration $a(t)$, velocity $v(t)$, and distance $x(t)$ from building A that are valid for the time interval $7 < t < 10$.

The velocity vector of a particle moving in the xy -plane has components given by

$$\frac{dx}{dt} = 14 \cos(t^2) \sin(e^t) \quad \text{and} \quad \frac{dy}{dt} = 1 + 2 \sin(t^2), \quad \text{for } 0 \leq t \leq 1.5.$$

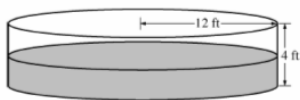
At time $t = 0$, the position of the particle is $(-2, 3)$.

- (a) For $0 < t < 1.5$, find all values of t at which the line tangent to the path of the particle is vertical.
- (b) Write an equation for the line tangent to the path of the particle at $t = 1$.
- (c) Find the speed of the particle at $t = 1$.
- (d) Find the acceleration vector of the particle at $t = 1$.

3)

4)

t	0	2	4	6	8	10	12
$P(t)$	0	46	53	57	60	62	63



The figure above shows an aboveground swimming pool in the shape of a cylinder with a radius of 12 feet and a height of 4 feet. The pool contains 1000 cubic feet of water at time $t = 0$. During the time interval $0 \leq t \leq 12$ hours, water is pumped into the pool at the rate $P(t)$ cubic feet per hour. The table above gives values of $P(t)$ for selected values of t . During the same time interval, water is leaking from the pool at the rate $R(t)$ cubic feet per hour, where $R(t) = 25e^{-0.05t}$. (Note: The volume V of a cylinder with radius r and height h is given by $V = \pi r^2 h$.)

- Use a midpoint Riemann sum with three subintervals of equal length to approximate the total amount of water that was pumped into the pool during the time interval $0 \leq t \leq 12$ hours. Show the computations that lead to your answer.
- Calculate the total amount of water that leaked out of the pool during the time interval $0 \leq t \leq 12$ hours.
- Use the results from parts (a) and (b) to approximate the volume of water in the pool at time $t = 12$ hours. Round your answer to the nearest cubic foot.
- Find the rate at which the volume of water in the pool is increasing at time $t = 8$ hours. How fast is the water level in the pool rising at $t = 8$ hours? Indicate units of measure in both answers.

Calculus Related AP problems

Solve the following with your group members, but make sure to record thoughts and conclusions on your own paper. Where justification is requested, make sure you justify (with mathematics, not loosey goosey opinions).

Let f be a function defined on the closed interval $-5 \leq x \leq 5$ with $f(1) = 3$. The graph of f' , the derivative of f , consists of two semicircles and two line segments, as shown above.

- (a) For $-5 < x < 5$, find all values x at which f has a relative maximum. Justify your answer.
 - (b) For $-5 < x < 5$, find all values x at which the graph of f has a point of inflection. Justify your answer.
 - (c) Find all intervals on which the graph of f is concave up and also has positive slope. Explain your reasoning.
 - (d) Find the absolute minimum value of $f(x)$ over the closed interval $-5 \leq x \leq 5$. Explain your reasoning.
- (07B)

